# **ORIGINAL RESEARCH ARTICLE**

# Models for estimation of solar irradiance in Zimbabwe: A statistical and machine learning approach

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#### ABSTRACT

The present study focused on the statistical development of solar irradiance predictive models for locations with limited solar irradiance measuring equipment. Multiple linear regression models were developed using both measured and satellite corrected meteorological data. The study chose easy to measure and access meteorological data for analysis and modelling. Multicollinearity and correlation analysis were performed to analyse the relationships among the independent and dependent variables. Statistical predictive models were developed, and the prediction accuracy of the developed models was analysed using the coefficient of determination ( $R^2$ ) and the Mean Absolute Percentage Error (MAPE). The results revealed a higher performance of the developed models compared to generic empirical models. The prediction MAPE for the three models developed were respectively 0.117 kWh/m<sup>2</sup>, 0.132 kWh/m<sup>2</sup> and 0.044 kWh/m<sup>2</sup> for H<sub>g</sub>, H<sub>b</sub> and H<sub>d</sub>. The models also had R<sup>2</sup> values of 0.895, 0.972 and 0.993 respectively for global horizontal irradiance (H<sub>g</sub>), direct normal irradiance (H<sub>b</sub>) and diffuse irradiance (H<sub>d</sub>). The developed models outperformed the generic models by a minimum of 5.74%. The study showed that it is more accurate to predict Global Horizontal Irradiance by summing the predicted component of H<sub>b</sub> and H<sub>d</sub>.

Keywords: solar irradiance; irradiance prediction; predictive modelling; meteorological parameters; regression analysis

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## **1. Introduction**

The economic and industrial growth happening in the world over has resulted in increased energy demand which in turn has increased the use of fossil-based energy systems thus destroying the environment and causing global warming. As a mitigating approach, there is a constant global shift from fossil energy systems in favour of renewable energy systems. Solar energy is one of these important clean energy sources that can alleviate the negative impacts of global warming<sup>[1]</sup>. New technologies in utilization of renewable energy particularly solar energy, as well as mitigation and adaptation are desirable in reducing pollution levels and mitigating global warming<sup>[2,3]</sup>.

Accurate solar irradiance data is especially important in the design, development, and utilization of solar energy technologies<sup>[4]</sup>. Therefore there is a need for accurate data on solar radiation although it is not readily available due to the absence of measuring equipment especially in developing countries<sup>[5]</sup>. This is due to the high cost of maintenance and calibration required for irradiance measuring instruments<sup>[6]</sup>.

Measured solar irradiance data is mostly important but, in its absence, models to obtain such data are useful in the deployment of solar energy systems<sup>[7]</sup>.

Models have been developed to estimate solar irradiance and these include empirical models and artificial intelligence based models<sup>[8]</sup>. Liu and Jordan<sup>[9]</sup> are among the pioneers in irradiance predictions. They studied the correlation between the monthly diffuse irradiance and global horizontal irradiance and established a 3rd order correlation based on clearness index. Similarly, Collares-Pereira and Rabl<sup>[10]</sup> developed a predictive 4th order polynomial using data from five locations in the USA and using the same approach, many other correlations were developed.

For example, Mecibah et al.<sup>[11]</sup> developed 11 models to estimate the mean monthly global horizontal irradiance using sunshine records and air temperature for six cities in Algeria. Their results revealed that sunshine based models had better performance compared to other models. Pai et al.<sup>[12]</sup> formulated a statistical model based on the Melo-Escobedo-Oliveira shadowing correction to estimate the anisotropic diffuse fraction from the clearness index. Their study reported an improved model with accuracy improvement from prediction error of 6% to 1.5%.

Feng et al.<sup>[13]</sup> developed four artificial intelligence-based models to estimate diffuse irradiance at two meteorological stations. The input parameters used were daily global horizontal irradiance, sunshine duration, daily extraterrestrial irradiance and the maximum possible sunshine duration. The performance of these models was found to be better than the empirical model by Iqbal<sup>[14]</sup>. Roderick<sup>[15]</sup> developed correlations between the diffuse fraction and clearness index using the daily global horizontal irradiance and the diffuse irradiance. A model was developed to estimate the monthly average daily diffuse radiation and it was found to have reasonable accuracy with an R<sup>2</sup> of 0.86.

Zimbabwe is rich in solar energy and has high potential for the establishment of solar farms which could possibly alleviate the acute energy deficit in the country. Despite having the solar resource, the measured solar irradiance data itself is not readily available and hence there is need for solar irradiance estimation models. For example, Hove et al.<sup>[16]</sup> expressed the need to estimate solar irradiance in Zimbabwe to make informed decisions in the deployment of solar energy systems. The present study seeks to establish multiple linear regression empirical models to estimate solar irradiance components i.e., the global horizontal irradiance, direct normal irradiance, and diffuse irradiance. This is based on the premise that solar irradiance data is not easily available despite being an important factor in solar system design<sup>[17,18]</sup>. To improve the accuracy of the prediction models, satellite data is correlated with measured data to establish a relationship between measured and satellite data. This is done to approximate measured data with satellite data using a correction factor and hence improve the accuracy of the developed models. Hove et al.<sup>[16]</sup> noticed the inaccuracies inherent in satellite measured data and hence the need for more accurate models. In the present study, models were developed specifically for Zimbabwe because generic models are less accurate in their prediction. Furthermore, empirical models are mostly location dependent and hence there is need to develop models specifically meant for each location. It is therefore important to explore novel methods in estimating solar irradiance<sup>[19]</sup>. Performance evaluation and estimation requires detailed information and data with regards solar radiation and its individual components. In this study, analysis of predictor variables was done, and special attention was made to use parameters which can be easily measured with simple instruments and those which can be obtained analytically.

## 2. Materials and methods

## 2.1. Location

Zimbabwe is a southern African country with abundant solar radiation with an annual global horizontal irradiance of 1857 kWh/m<sup>2</sup> to 2257 kWh/m<sup>2</sup> and an average of 6.7 to 8.9 sun hours per day<sup>[20]</sup>.

Data were obtained from 11 different locations in Zimbabwe from each grid point as shown in **Figure 1**. The 11 different locations were meant to provide a full coverage of aggregated data for the whole country. Zimbabwe is a landlocked country with a tropical savanna climate characterized by two major seasons i.e., summer and winter.



Figure 1. Map of Zimbabwe with some selected locations<sup>[21]</sup>

The winter season is mostly dry and in some parts of the winter it is often characterized by heavy clouds with sporadic light showers across the country. Generally, the winter season spans from the month of May to the month of September while summer begins in October to April. The average precipitation accumulates to 25 mm during winter season while it can accumulate to 800 mm in the summer season. The average temperatures for the winter and summer season are respectively 17 °C and 24 °C.

#### 2.2. Meteorological data

Meteorological data of 10 different parameters were obtained on NASA Solar Energy and Surface Meteorology (https://power.larc.nasa.gov/data-access-viewer/, accessed on 9 November 2022). Typical Meteorological Year Data were obtained from 2011 to 2021 for the following parameters, Pressure, Temperature, Relative Humidity (RH), Declination ( $\delta$ ), Solar Noon Time, Clearness Index (K<sub>T</sub>), Percentage Cloud Cover, Clear Sky Clearness Index, Daily Average Precipitation, Day Length, Sunset Hour Angle ( $\omega$ ), Cumulative Monthly Precipitation, Direct Normal Irradiance (DNI or H<sub>b</sub>) and Diffuse Irradiance (DI or H<sub>d</sub>). Ground measurements were also collected for a year from 6 locations evenly spread across the country using a Davis Vantage pro 2 plus weather station.

#### 2.3. Data treatment and pre-processing

Python v3.0 was used in the data cleaning process. Incomplete records were removed from the data set and replaced with an average data value for that parameter. The data in which the Global Horizontal Irradiance (GHI or  $H_g$ ) or direct normal irradiance exceeded the extraterrestrial radiation were also removed and replaced with average values. Data sets where  $K_T$  and the diffuse fraction were greater than 1 were also removed. The collected data was divided into training and validation data sets in a ratio of 75:25 respectively for training and validation.

#### 2.4. Dimensionality reduction and parameter correlation analysis

Dimensionality reduction was performed to reduce the number of variables to be used in the modelling process. This approach was used to retain the most important parameters in the predictive modelling process

and eliminate variables that are duplicate, misleading or inappropriate<sup>[22,23]</sup>. The performance of developed models often increases with a reduction in the number of predictor variables<sup>[24]</sup>. Boruta algorithm was implemented for feature ranking and selection and uses feature importance scoring which is based on Random Forests algorithm. This algorithm has the advantage of selecting features that are statistically significant. Boruta algorithm is different from other feature selection techniques in that rather than ordering, it has a sharp classification of features and it also retains all relevant variables for the decision<sup>[25,26]</sup>. This algorithm uses shadows which are basically copies of original features with randomly added values intended to retain their distribution while their importance is removed. A complete description and implementation of this algorithm is outlined in the references<sup>[27,28]</sup>. Boruta algorithm, however, cannot remove multicollinearity as such parameter correlation was performed.

Parameter correlation and curve fitting was performed in this study for all the 10 parameters using Veusz v3.4 software (https://veusz.github.io/)<sup>[29]</sup>. Relationships were established between each of the solar radiation components and the different meteorological parameters. Curve fitting was done, and performance metrics were recorded to ascertain the relationship between the parameters being investigated and solar irradiance. The models evaluated in the curve fitting process were linear, quadratic, cubic, 4<sup>th</sup> order, hyperbolic and logarithmic. All these were evaluated for each parameter relation to H<sub>g</sub>, H<sub>d</sub> and H<sub>b</sub>. The model/function that gave the highest value or  $\mathbb{R}^2$  was selected as the representative model relating the variable to the solar irradiance component. All the 10 parameters used in this study were evaluated for their contribution in the prediction of solar irradiance. Multicollinearity, a common factor in empirical analysis was also investigated among the parameters to minimise the possibility of increasing the standard error and other complexities emanating from multicollinearity<sup>[30–32]</sup>. This was intended to identify those parameters which are also correlated in a view of eliminating redundancy and unnecessary complexity in the developed model. All parameters with a correlation coefficient greater than 0.8 had one of them eliminated. The criteria for elimination were based on retaining the parameter whose values are easily obtainable or easily measurable.

#### **2.5. Modelling**

A relationship was established between the ground measured data and satellite data to determine a correction factor used to estimate ground measured parameters from satellite data. Ground measured data from the six selected locations across the country were averaged for all the measured parameters and similarly, the satellite data were also averaged for the 11 locations. A correlation was developed between these two data sets to develop correction factors for each parameter. The correction factors were used to correct the satellite data to match ground measured data. This was done to improve the prediction accuracy of the model in the estimation of ground measured data.

Multiple linear regression models were developed to predict Global Horizontal Irradiance, Direct Normal Irradiance, and Diffuse Irradiance. The models were of the form shown by Equation 1 where y is the dependent variable,  $x_1, x_2, ..., x_n$  are the independent predictor variables while  $\beta_0, \beta_1, \beta_2, ..., \beta_n$  are constants and  $\varepsilon$  is the prediction error. The different measured parameters were used in the modelling process. Information from parameter correlation was collected and used in modelling. As such Vieusz v3.4 software was used in the modelling and data fitting process.

$$y = \beta_0 + x_1 \beta_1 + x_2 \beta_2 + \ldots + x_n \beta_n + \varepsilon \tag{1}$$

The variables selected through dimensionality reduction and parameter correlation analysis were used in the modelling process. The predicted values of solar irradiance were compared to the measured values to check the performance of the predictive model. The performance of the models were also compared to other empirical models including the model by Page<sup>[33]</sup> (Equations 2–4) and Liu and Jordan<sup>[9]</sup> (Equation 5) where  $\overline{H_g}$ ,  $\overline{H_d}$ ,  $\overline{H_o}$ ,  $\overline{S}$ ,  $\overline{S}_{max}$  are respectively the monthly average daily values for global horizontal irradiance, diffuse irradiance, extraterrestrial irradiance, sunshine hours and maximum possible sunshine hours. Isc is the solar constant equal

to 1367 W/m<sup>2</sup> while a and b are constants normally obtained by regression analysis.  $\omega_s$  is the sunset hour angle,  $\phi$  is the latitude of the location while  $\delta$  is the declination angle and is given by Equation 4.

$$\frac{\overline{H_g}}{\overline{H_o}} = a + b \left( \frac{\overline{S}}{\overline{S}_{max}} \right)$$
(2)

$$H_o = \frac{12}{\pi} I_{sc} \left( 1 + 0.033 \cos \frac{360n}{365} \right) \int_{-\omega_s}^{+\omega_s} (\sin\phi\sin\delta + \cos\phi\cos\delta\cos\omega) \, d\omega \tag{3}$$

$$\delta = 23.45 \sin\left(\frac{360n}{365}(284+n)\right) \tag{4}$$

$$\frac{\overline{H_d}}{\overline{H_g}} = 1.390 - 4.027 \left[ \frac{\overline{H_d}}{\overline{H_g}} \right] + 5.531 \left[ \frac{\overline{H_d}}{\overline{H_g}} \right]^2 - 3.108 \left[ \frac{\overline{H_d}}{\overline{H_g}} \right]^3$$
(5)

## **3. Results**

#### **3.1. Dimensionality reduction**

Dimensionality reduction performed using Boruta algorithm resulted in the selection of parameters outlined in **Table 1**. The algorithm chose parameters with an apparently low  $R^2$  for inclusion into the model. This is the strength of the algorithm because such parameters would have been left out if simple regression was used to select parameters. Using Boruta algorithm, only relative humidity was selected for the prediction of global horizontal irradiance (H<sub>g</sub>). The selected parameters for direct normal irradiance (H<sub>b</sub>) were % cloud cover, cumulative precipitation, clearness index, relative humidity, sunset hour angle, declination and temperature. Likewise, the selected parameters for diffuse irradiance (H<sub>d</sub>) were % cloud cover, cumulative precipitation, clearness index, relative humidity, pressure, sunset hour angle and temperature. Details of selected parameters are shown in **Table 1** where yes represent selected parameter and no represent non-selected parameter.

		Dependent variable		
	Parameter	$\mathbf{H}_{\mathbf{g}}$	$\mathbf{H}_{\mathbf{b}}$	$\mathbf{H}_{\mathbf{d}}$
1	% Cloud cover	No	Yes	Yes
2	Cumulative precipitation	No	Yes	Yes
3	Day length	No	No	Yes
4	Declination	No	Yes	Yes
5	Clearness index	No	Yes	Yes
6	Relative humidity	Yes	Yes	No
7	Pressure	No	No	Yes
8	Sunset hour angle	No	Yes	Yes
9	Temperature	No	Yes	Yes
10	Solar noon time	No	No	No

Table 1. Selected parameters.

Although the Boruta algorithm was able to select all relevant parameters, it selects all the parameters including parameters correlated to other features. As such, parameter correlation was performed to identify correlations among parameters themselves.

#### **3.2. Parameter correlation**

A parameter correlation matrix was developed and analysed for multicollinearity and their correlation with the irradiance components i.e.,  $H_d$ ,  $H_b$  and  $H_g$ . The results are shown in **Figure 2** and **Table 2** where DNI, GHI, DI,  $\omega_s$  and  $K_t$  are respectively Direct Normal Irradiance, Global Horizontal Irradiance, Diffuse Irradiance, Sunset Hour Angle and Clearness Index. There was a good correlation between  $H_g$  and relative humidity with a coefficient of determination ( $R^2$ ) of 0.78. However, the relation between  $H_g$  and all the other parameters was weak and the  $R^2$  values were less than 50%. All the ten parameters analysed had  $R^2$  values above 50% for their relationship with  $H_d$ . The notable parameters with a strong relation with  $H_d$  were % cloud cover, cumulative precipitation, day length, declination,  $K_T$ , pressure, temperature and sunset hour angle.  $H_b$  had a strong relationship between  $H_g$ ,  $H_b$ , and  $H_d$  with % cloud cover, cumulative precipitation and clearness index is shown in **Figures 2–5**. On the other hand, the relationship between solar noon time and,  $H_g$ ,  $H_b$ , and  $H_d$  was poor as shown in **Figure 6**.



Figure 2. Parameter correlation matrix.

		Correlation (R <sup>2</sup> )		
	Parameter	$\mathbf{H}_{\mathbf{g}}$	H <sub>b</sub>	$\mathbf{H}_{\mathbf{d}}$
1	% Cloud cover	0.41	0.94	0.94
2	Cumulative precipitation	0.46	0.96	0.92
3	Day length	0.25	0.86	0.78
4	Declination	0.25	0.86	0.61
5	Clearness index	0.31	0.97	0.89
6	Relative humidity	0.78	0.59	0.74
7	Pressure	0.14	0.72	0.45
8	Sunset hour angle	0.25	0.86	0.56
9	Temperature	0.28	0.65	0.29
10	Solar noon time	0.41	0.51	0.39

Table 2. Coefficients of determination in parameter correlation.



Figure 3. Relationship between (a)  $H_{g},$  (b)  $H_{b}$  and (c)  $H_{d}$  with % cloud cover.



Figure 4. (Continued).



Figure 4. Relationship between (a)  $H_g$ , (b)  $H_b$  and (c)  $H_d$  with cumulative precipitation.



Figure 5. Relationship between (a)  $H_g$ , (b)  $H_b$  and (c)  $H_d$  with  $K_T$ .



Figure 6. Relationship between (a)  $H_g$ , (b)  $H_b$  and (c)  $H_d$  with solar noon time.

There was also a strong relationship between % cloud cover with  $H_d$  and  $H_b$  whereas the relationship was relatively weaker with  $H_g$ . As shown by **Figure 3**, increasing the % cloud cover had an effect of reducing  $H_b$  and increasing  $H_d$  which is expected. The study also revealed a strong relationship between precipitation and,  $H_b$  and  $H_d$  while the relationship was somewhat weaker with  $H_g$ .  $H_b$  had a linear relationship with precipitation while  $H_d$  had a somewhat quadratic relationship. As the precipitation increased,  $H_b$  reduced while  $H_d$  increased with an overall effect of reducing  $H_g$  in a similar way to % cloud cover.

The relationships between day length and,  $H_d$  and  $H_b$  were relatively strong with respective linear and quadratic relationships. However, the relationship between day length and  $H_g$  was weak with a correlation of -0.19. As day length increases, there was an overall increase in  $H_d$  while as day length increased beyond 12 hours, there was no significant increase in  $H_b$ . On the other hand, the analysis of declination indicated that it had similar relations as those of day length. The relationship between declination and,  $H_b$  and  $H_d$  had  $R^2$  of respectively 0.61 and 0.86. A similar relationship was observed for the sunset hour angle. Furthermore, there is less  $H_d$  in winter due to relatively clear skies.  $K_T$  also has a strong relationship with  $H_b$  and  $H_d$ . The  $R^2$  values for  $K_T$  and,  $H_b$  and  $H_d$  are respectively 0.97 and 0.89.

Analysis of pressure and temperature showed a good correlation with  $H_d$  while its was weak with  $H_b$  and  $H_g$ . There is also a notable increase in  $H_d$  with increasing temperature. Relative humidity is also an important

factor with a strong relationship with  $H_g$  and  $H_b$ . Solar noon time had no significant relationship with solar irradiance.

#### 3.3. Modelling and analysis

The study analyzed multicollinearity among the parameters and several variables were found to be correlated and these include precipitation and cloud cover, and, day length, declination and sunset hour angle. For example, the relationship between precipitation and cloud cover had an  $R^2$  of 98.24% and day length had a perfect correlation with declination with  $R^2$  of 99%. Further,  $K_T$  also had a strong correlation,  $R^2 = 0.98$  with precipitation and was also well correlated with cloud cover. Having analyzed all parameters with multicollinearity analysis, the variables in **Table 3** were selected for modelling.

	Parameters
$H_{g}$	Relative humidity
$H_{b}$	Relative humidity, declination, temperature and cumulative precipitation
$H_{d}$	Pressure, temperature, cumulative precipitation and declination

Meteorological data was measured from 6 different locations across Zimbabwe for one year. Monthly averaged values of the meteorological data were obtained from the measured data. The monthly averaged satellite meteorological data from 11 locations was also obtained. The collected data were relative humidity, pressure, temperature and precipitation. Declination was computed from Equation 4. The two data sets i.e., satellite data and ground measured data were correlated to obtain a correction factor to transform satellite data to approximate ground measured data. The relationships between measured data (y) and satellite data (x) are depicted by Equations 6–9.

Pressure: 
$$y = 0.951x + 3.385$$
 (6)

Temperature: 
$$y = 1.004x - 0.443$$
 (7)

Relative humidity: 
$$y = 1.011x - 2.539$$
 (8)

Cumulative precipitation: 
$$y = 0.906x + 5.592$$
 (9)

Satellite data were converted into ground measured data and multiple linear regression was employed to correlate the meteorological parameters to  $H_g$ ,  $H_b$  and  $H_d$ . The developed models are as shown in Equations 10–12. Let pressure, temperature, relative humidity, declination and precipitation be respectively represented by  $x_1$ ,  $x_2$ ,  $x_3$ ,  $x_4$  and  $x_5$ . The study revealed that even those parameters with a lower correlation value when correlation analysis was done are important in the development of a multiple linear regression. This phenomenon was also explained by Smith<sup>[34]</sup>. The Boruta method used for screening parameters showed that parameters with low correlation with the predicted variable can still have some importance and thus can be incorporated into the multiple linear regression model. For example, correlation analysis showed that  $H_d$  has a somewhat weaker relationship with relative humidity, but the parameter selection algorithm still picked it as an important parameter hence even the less correlated variables are also important in predictive modelling.

$$H_a = 9.72 + 0.0354x_3 \tag{10}$$

$$H_b = 6.072 + 0.127x_2 - 0.0462x_3 + 0.0544x_4 + 0.0001x_5 \tag{11}$$

$$H_d = -0.225 + 0.00013x_1 + 0.0787x_2 - 0.0002x_3 + 0.00656x_4 + 0.005x_5$$
(12)

The validation of the models was done using measured data and the graphs for predicted vs actual were plotted as in **Figure 6**. The models were found to have good performance in their prediction with  $R^2$  values of 0.895, 0.972 and 0.983 respectively for  $H_g$ ,  $H_b$  and  $H_d$  which was higher compared to results reported by Brahma and Wadhvani<sup>[35]</sup> and comparable to the results by Singla et al.<sup>[36]</sup>. The coefficients of multiple

regression for the models were respectively 0.946, 0.986 and 0.997 for  $H_g$ ,  $H_b$  and  $H_d$  and this was comparable to studies in literature<sup>[37–39]</sup>. The Mean Absolute Percentage Errors (MAPE) were respectively 0.117 kWh/m<sup>2</sup>, 0.132 kWh/m<sup>2</sup> and 0.044 kWh/m<sup>2</sup> for  $H_g$ ,  $H_b$  and  $H_d$ . These metrics show a very close agreement between measured and predicted values. The prediction errors are relatively small while the R<sup>2</sup> values are high indicating good performance of the predictive models. Comparison was made with established models in literature proposed by Page<sup>[33]</sup> for  $H_g$  prediction shown by Equation 1 while the Diffuse Irradiance was predicted using a model by Liu and Jordan<sup>[9]</sup> shown by Equation 5. Comparison with these models revealed better performance of the developed models compared to existing empirical models. For example, the developed models were better by 9.71%, 11.33% and 5.74% for predicting  $H_b$ ,  $H_d$  and  $H_g$  respectively. This is attributed to the fact that exact location data were used in the development of these models.

#### 4. Discussions

There was also a strong relationship between % cloud cover with  $H_d$  and  $H_b$  whereas the relationship is relatively weaker with  $H_g$ . Cloud cover has an overall effect of reducing  $H_g$  mainly because most of the incoming irradiance will be reflected into space thus reducing solar irradiance reaching the surface. Precipitation was also found to affect  $H_d$  and  $H_b$  in that it reduces the incident beam irradiance ( $H_b$ ) while amplifying the presents of diffuse irradiance ( $H_b$ ).

As day length increases, there was an overall increase in  $H_d$  while as day length increased beyond 12 hours, there was no significant increase in  $H_b$ . This is because day length increases by an early sunrise and a delayed sunset. As expected, this increase will only impact the  $H_d$  component because there is a low  $H_b$  component in the morning and sunset. The relationship between declination and,  $H_b$  and  $H_d$  had  $R^2$  of respectively 0.61 and 0.86. This is because declination is negative in summer and positive in winter for Zimbabwean locations. A similar relationship was observed for the sunset hour angle. Despite having shorter days in winter, the clear skies have an effect of increasing the  $H_b$  component while the  $H_d$  component reduces unlike in summer where there is more rain and cloud cover. This is also confirmed by low values of  $H_b$  in the wettest periods in summer which are December and January. Furthermore, there is less  $H_d$  in winter due to relatively clear skies.  $K_T$  also has a strong relationship with  $H_b$  and  $H_d$ . There was a positive relation between  $H_b$  and  $K_T$  because as the skies become clearer, there is more Direct Normal Irradiance reaching the earth while Diffuse Irradiance is reduced. The  $R^2$  values for  $K_T$  and,  $H_b$  and  $H_d$  are respectively 0.97 and 0.89. This could be the reason why many empirical models developed in literature mainly considered  $K_T$  as a key parameter.

Pressure and temperature had a good correlation with  $H_d$  while its was weak with  $H_b$  and  $H_g$  and a notable increase in  $H_d$  with increasing temperature was noted and this is attributed to the fact that cloud cover has a greenhouse effect which increase temperature and reduce  $H_b$  while increasing  $H_d$ . Relative humidity is also an important factor with a strong relationship with  $H_g$  and  $H_b$ . Increasing relative humidity reduces both  $H_g$  and  $H_b$  due to the increased particulate matter in the atmosphere caused by the presents of water droplets which reflect and scatter incoming irradiance.

## 5. Conclusions and future studies

The study seeks to develop irradiance prediction models which are critical in forecasting solar irradiance in design and maintenance of solar plants. Machine learning and statistical approaches were adopted in model development to increase the prediction accuracy. The location dependent models developed predict solar irradiance in the absence of solar irradiance data by making use meteorological data.

The study analyzed the influence of each of the selected meteorological parameters on solar irradiance. Boruta algorithm was used to select all the relevant parameters while multicollinearity and correlation analysis were also performed to analyse the impact of each of the parameters on one another. Models were developed to predict solar irradiance and the following were noted:

- The individual correlation of H<sub>g</sub> with the parameters analysed only showed a strong correlation with relative humidity.
- Increasing the day length does not significantly increase  $H_b$  but has an overall effect of increasing  $H_g$ .
- Lower correlation between solar irradiance and a selected parameter does not necessarily mean the parameter is insignificant. The parameter selection algorithm used indicated that even the less correlated parameters could still be important in predictive modelling.
- The study noted that direct prediction of Global Horizontal Irradiance using meteorological variables is less accurate compared to using the sum of predicted Diffuse Irradiance and Direct Normal Irradiance.

The developed models were however dependent on satellite measured historical data which may not take into consideration the constant effect of global warming. It is therefore recommended that models be developed that take real-time data as input.

# **Author contributions**

Conceptualization, KC and RM; methodology, KC; software, RM; validation, RA and CE; formal analysis, KC; investigation, KC; resources, CE and RA; data curation, RM; writing—original draft preparation, KC; writing—review and editing, CE; visualization, RM; supervision, CE; project administration, CE; funding acquisition, CE. All authors have read and agreed to the published version of the manuscript.

# **Conflict of interest**

The authors declare no conflict of interest.

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